The purpose of this paper is to provide an overview of the sound power radiation mechanism of air-core reactors and to describe the method that is used to calculate sound power by using the electrical load. Sound power radiation of an air-core reactor is related to the alternating current harmonics, the mechanical tension stiffness and, most importantly, the breathing mode resonance. An analytical model that is based on electrical loads and mechanical properties of the air-core reactor is developed to calculate radial and axial forces caused by the radial and axial magnetic induction fields. This study employs the hemispherical spreading theory, which is a simple and common method that is used to predict sound propagation. Additionally, a numerical model is proposed. In this, the excitation of the acoustic field that surrounds the reactor is introduced by considering the radial and axial displacements of the reactor’s windings, as the windings are subjected to the action of the radial and axial electromagnetic forces. Finally, a comparison is presented between analytical and numerical models and it is observed that the models are correlated.

NOMENCLATURE

\(B\)  
- magnetic induction field

\(B_{radial}\)  
- radial magnetic induction field

\(B_{axial}\)  
- axial magnetic induction field

\(B_{avg,z}\)  
- average magnetic induction field at \(z\) direction

\(B_{avg,x}\)  
- average magnetic induction field at \(x\) direction

\(c_0\)  
- speed of sound in air

\(d\)  
- infinitesimal element

\(E\)  
- equivalent Young’s modulus

\(E_{fib}\)  
- Young’s modulus of the fiberglass

\(e\)  
- thickness of the winding

\(e_{fib}\)  
- thickness of the fiberglass

\(e_{iso}\)  
- thickness of the insulation

\(F\)  
- electromagnetic force

\(F_{avg,x}\)  
- average force at \(x\) direction

\(F_{axial}\)  
- axial electromagnetic force

\(F_{radial}\)  
- radial electromagnetic force

\(F_{Z,avg}\)  
- average force at \(z\) direction

\(f\)  
- frequency of the current

\(G_{xy}\)  
- shear modulus at plane \(xy\)

\(G_{xz}\)  
- shear modulus at plane \(xz\)

\(G_{yz}\)  
- shear modulus at plane \(yz\)

\(H\)  
- average height of the winding

\(h_{ws}\)  
- height of the reactor without the spiders

\(I_{eff}\)  
- effective current

\(i\)  
- electrical current

\(K\)  
- stiffness of a mechanical system

\(K_{eq}\)  
- equivalent stiffness

\(K_{fib1}\)  
- stiffness of fiber layer 1

\(K_{fib2}\)  
- stiffness of fiber layer 2

\(l\)  
- height of the material

\(l_{ms}\)  
- perimeter of measurement surface

\(L_P\)  
- average sound pressure

\(L_P\)  
- sound pressure level

\(L_W\)  
- sound power level

\(M\)  
- mass of the winding

\(N\)  
- number of turns per unit of length

\(nbr\)  
- total average number of turns in the winding

\(p\)  
- sound pressure

\(p_0\)  
- reference sound pressure

\(R\)  
- average radius of the winding

\(R_e\)  
- external radius of the winding

\(R_i\)  
- internal radius of the winding

\(r\)  
- distance point to source

\(r_{sr}\)  
- distance source-receiver

\(S\)  
- surface of contact between two materials

\(S_m\)  
- surface area of measurement

\(S_W\)  
- sound radiating surface

\(S_0\)  
- reference area

\(t\)  
- time

\(\nu_{rad}\)  
- average radial speed of the winding

\(W\)  
- radiated sound power

\(W_0\)  
- reference power
1. INTRODUCTION

The population growth and the increasing use of electricity demands the construction of substations for power transmission near major consumption centers. Due to this, the surrounding communities are affected by the noise generated by these stations. Substation noise is a problem not only because of the high power levels, but also because of the presence of tonal noises that can cause discomfort. Among the main sources of noise in these industrial plants are transformers, capacitors, and air-core reactors.

When considering the impact of audible noise emanating from a high voltage direct current (HVDC) station, the alternating current (AC) filter reactors, and the HVDC smoothing reactor are the main types of air-core reactors that need to be considered. According to the International Council on Large Electric Systems, the forces resulting from the interaction between the current flow through the reactor and its magnetic induction cause the vibration of reactor surfaces. Some researchers consider that, from the viewpoint of noise generation, vibration amplitude and area of radiating surface determine the sound power generated by air-core reactors.

There is a lot of interest in determining the forces acting in the radial direction because they induce bending waves on reactor surface, while axial forces excite longitudinal waves. In the case of air-core reactors, the radiation efficiency of bending waves is greater than the longitudinal waves.

This paper describes the mechanism of sound generation in air-core reactors. Two models for calculating the sound power level of reactors are presented: the analytical model estimates the sound power from the radial and axial force created by the axial and radial magnetic field that acts over the reactor and the numerical model uses the radial and axial forces calculated by the analytical model as the excitation of the acoustic field that surrounds the reactor. The analytical and numerical results of a typical configuration of an air-core reactor used in HVDC system are compared with experimental results.
The vibration amplitude and size of the sound radiating surface of the apparatus essentially determine the sound power. Therefore, the sound emission of an air-core reactor is governed by the magnitude of the winding vibration in the radial direction, since the winding represents the main part of the radiating surface. The contribution of axial winding vibrations and that of other components to the total sound emitted is relatively low.

The results of an air-core reactor, which has the configuration usually found in HVDC stations, are presented in this paper. It has one winding, natural cooling, and its winding is formed by one layer of insulated aluminum conductor. Among the conductors, there are layers of fiberglass with epoxy resin. Other geometrical characteristics of the reactor are shown in Table 1.

### 3. SOUND GENERATION MECHANISM

Alternating currents through the reactor simultaneously produce an electric field due to the electric charges and a magnetic field because of the flowing current. The resulting electromagnetic interaction results in the creation of an electromagnetic force, which causes the vibration of the walls.

#### 3.1. Analytical Model

The determination of the expression of the magnetic induction field in all points of the winding involves the solution of complex numerical equations, which does not allow for a simple analytical expression of the field according to the parameters of the system. Therefore, in order to develop an analytical model, some hypothesis are assumed, and the magnetic induction field is broken up in two parts: the radial magnetic induction field $B_{\text{radial}}$, and the axial magnetic induction field $B_{\text{axial}}$. This form will enable the division of the problem into two parts: the radial mode involves the calculation of the axial field, which causes a radial electromagnetic force $F_{\text{radial}}$ and the axial mode, which involves the calculation of the radial field and causes an axial electromagnetic force $F_{\text{axial}}$.

The determination of the expressions of the radial and axial fields will be carried out by the use of the following relations:6

a) The Biot-Savart Law expresses the value of the magnetic induction field $\mathbf{B}$ created by an infinitesimal element of
current \( \mathbf{dl} \) in a distant point \( r \) of the source.

\[
\mathbf{B}(t) = \frac{\mu_0}{4\pi} i(t) \int \frac{\mathbf{dl} x_0}{r^3};
\]  

(1)

where \( \mu_0 \) is the permeability of free space. The small circle on the integral sign indicates that the path of integration is a closed loop. Since the current has a sinusoidal behavior with respect to time, it can be expressed as:

\[
i(t) = \sqrt{2} I_{\text{eff}} \sin(\omega t);
\]

(2)

where, \( I_{\text{eff}} \) is the effective current (A) and \( \omega \) is angular frequency of the current (rad/s).

b) Ampère’s Law provides a method for evaluating \( B \) fields when the current distribution has some simplifying features. The law relates the path integral of the magnetic induction field \( B \) around a closed loop to the total current \( i(t) \) passing through the loop. In mathematical terms, this can be written:

\[
\oint \mathbf{B}(t) \mathbf{dl} = \mu_0 i(t).
\]

(3)

c) The electromagnetic force equation is defined by:

\[
\mathbf{F}(t) = \oint i(t) \mathbf{dl} \times \mathbf{B}.
\]

(4)

3.1.1. Radial mode

To simplify the development of equations, the value of the axial induction field is calculated on the axis of the winding, as illustrated in Fig. 3. It will be uniformly distributed into the winding and the conductors. The magnetic induction field in a point \( P \) of the axis of the winding, Eq. (5), can be estimated by the initial calculation of the field on the axis of one turn using the Biot-Savart Law, which is followed by the extrapolation of the initial calculation of the field on the axis of one turn using the average radius of the winding, \( H \) is the height of the winding (\( H = nbr \cdot \Theta \)), and \( \omega \) is the angular frequency of the current.

\[
B(z,t) = \frac{\sqrt{2} \mu_0 I_{\text{eff}} N}{2} \left[ \frac{z}{(R^2 + z^2)^{1/2}} + \frac{(H - z)}{(R^2 + (H - z)^2)^{1/2}} \right] \sin(\omega t); 
\]

(5)

where, \( \mu_0 \) is the permeability of free space, \( I_{\text{eff}} \) is the effective current, \( N \) is the number of turns per unit of length (\( N = 1/\Theta \)), \( z \) is the distance in Z axis of the point \( P \), \( R \) is the average radius of the winding, \( H \) is the height of the winding (\( H = nbr \cdot \Theta \)), and \( \omega \) is the angular frequency of the current.

Observe that the axial induction field is maximum in the center of the winding and minimum at the two ends.

To avoid the complex integration of Eq. (5) over the height of the winding, the following calculation of the average axial magnetic induction field, Eq. (6), will be used:

\[
B_{\text{axial}}(t) = B_{\text{avrg},z}(t) = \frac{\sqrt{2} \mu_0 I_{\text{eff}} N}{H} \left[ (R^2 + (H - z)^2)^{1/2} - R \right] \sin(\omega t).
\]

(6)

Because the turns of the winding are subjected to the average magnetic induction field \( B_{\text{axial}} \) (constant in all inner points of the winding), each turn of the winding is subjected to the same radial linear force \( F_{\text{radial}} \) determined by Eq. (7).

\[
F_{\text{radial}}(t) = F_{\text{avrg},x}(t) = \frac{2 \mu_0 I_{\text{eff}} N}{H} \left[ (R^2 + (H - z)^2)^{1/2} - R \right] \sin^2(\omega t).
\]

(7)

The radial force is expressed in N/m and has the following properties:

a) The force is unidirectional and repulsive, i.e., no deformation towards the inner part of the winding;

b) The force is proportional to the square of the current, \( I_{\text{eff}} \), and proportional to the number of turns per unit of length \( N \);

c) The frequency of the average force is twice the frequency of the current.

Figure 4 shows the distribution of the radial force acting over one turn of the winding. \( F_N \) is the normal force of traction that acts over the thickness of the turn.

Making the vertical balance of the forces that act in the Y direction, the following equation for the radial displacement of the winding is:

\[
\Delta R(t) = \frac{2 \mu_0 I_{\text{eff}} R^2}{nbrEe} \left[ (R^2 + (nbr \varphi)^2)^{1/2} - R \right] \sin^2(\omega t);
\]

(8)

where, \( nbr \) is the total average number of turns in the winding, \( \varphi \) is the conductor diameter, \( e \) is the thickness of the winding, \( E \) is an equivalent Young’s modulus calculated based on the total area of the winding subjected to the normal force and the total areas of the conductor and fiberglass. Young’s modulus of the aluminum and the fiberglass are 7.2×10^10 N/m^2 and 3.0×10^10 N/m^2, respectively.
Deriving the expression of radial displacement with respect to time yields the expression of the average radial speed of the winding as follows:

\[
\nu_{\text{rad}}(t) = \frac{4\mu_0 I_{\text{eff}}^2 R^2 \pi f}{\pi f_{\text{br}}^3} \left[ (R^2 + (nb r\varphi)^2)^{0.5} - R \right] \sin(2\omega t); \quad (9)
\]

where \( f \) is the frequency of the current in hertz.

### 3.1.2. Axial mode

For example, considering the winding formed by four turns located parallel one against each other, as shown in Fig. 5.

The radial induction field that acts over the first turn is equivalent to the sum of the contributions of the fields created by the others turns. The field that acts over the second turn is null because of the cancelation of the induction of the first and third turns. So, it is possible to conclude that the resulting field that acts over the median turn is null. Using these conclusions and Ampere’s Law for a linear conductor, the radial induction field in a point located at \( z = 0, z < H/2, z = H/2, z > H/2 \) and \( z = H \), may be obtained. These expressions utilize convergent series that have hard solutions. To simplify the analytical calculation procedure, these expressions are reduced to an expression that can be integrated on the half height of the winding in order to obtain the average value of the radial magnetic induction field on both sides.

\[
B_{\text{radial}}(t) = B_{\text{avg},x}(t) = \pm \frac{\sqrt{2\mu_0 I_{\text{eff}}^2}}{4\pi f} \ln(nb r\varphi) \sin(\omega t) \rightarrow (+)
\]

when \( z < H/2 \) or \((-)\) when \( z > H/2; \quad (10)\)

\[
B_{\text{radial}}(t) = B_{\text{avg},x}(t) = 0 \rightarrow z = H/2; \quad (11)
\]

where, \( \varphi \) is the diameter of the conductor and \( nb r \) is the total average number of the turns in the winding.

Therefore, consider again that the winding is subject to average radial induction field. Each turn undergoes the same linear force:

\[
F_{\text{axial}}(t) = F_{Z,\text{avg}}(t) = \pm \frac{\mu_0 I_{\text{eff}}^2}{2\pi f} \ln(nb r\varphi) \sin^2(\omega t) \rightarrow (+)
\]

when \( z < H/2 \) and \((-)\) when \( z > H/2; \quad (12)\)

\[
F_{\text{axial}}(t) = F_{Z,\text{avg}}(t) = 0 \rightarrow z = H/2. \quad (13)
\]

The axial force is expressed in N/m and has the following properties:

- a) The force is proportional to the square of the current \( I_{\text{eff}} \).
- b) The frequency of the average force is twice the frequency of the current.
- c) The distribution of the axial force compresses the winding.

The axial force compresses the winding, therefore in this mode of deformation the winding can be seen as a mass-spring-mass-spring assembly, as shown in Fig. 6a. The first mass consists of the sum of the mass of the conductor and fiberglass while the second mass corresponds to the sum of the mass of the insulator and fiberglass.

The general expression that defines the stiffness \( K \) of a mechanical system is:

\[
K = \frac{E S}{l}. \quad (14)
\]

In this case, \( l \) corresponds to the height of the material, \( S \) indicates the contact surface between two materials, and \( E \) is Young’s modulus of the material. The following stiffness \( K_{Al}, K_{fib1}, K_{iso}, \) and \( K_{fib2} \) will exist for one turn.

The contact surface between conductor and insulator is weaker than the contact surface between fiberglass layers, so the stiffness \( K_{Al} \) and \( K_{iso} \) can be neglected when compared...
to the stiffness $K_{fib1}$ and $K_{fib2}$. Once the two springs are in series, the equivalent stiffness of the system is:

$$K_{eq} = \frac{K_{fib1}K_{fib2}}{K_{fib1} + K_{fib2}}. \quad (15)$$

Young’s modulus of the material that forms the turn can be obtained by replacing the expression of the equivalent stiffness in Eq. (14), and assumes that $l$ is equal to the diameter of the turn.

$$E = \frac{K_{eq}\varphi}{2\pi e R}. \quad (16)$$

It may be observed that the value of Young’s modulus for the radial mode and axial mode are different.

As in radial mode, using the definition for Young’s modulus, the expression for the axial displacement of the winding $\Delta H$ can be obtained:

$$\Delta H(t) = \frac{\mu_0 f^2}{2\pi E_{fib} e_{fib}} \ln(nbr) \sin^{2}(\omega t); \quad (17)$$

where, $E_{fib}$ and $e_{fib}$ are respectively Young’s modulus and the thickness of the fiberglass.

Deriving the expression of the axial displacement in respect to time, the expression of the average axial speed of the winding can be obtained:

$$v_{axi}(t) = \frac{f\mu_0 f^2}{E_{fib} e_{fib}} \ln(nbr) \sin(2\omega t). \quad (18)$$

### 3.1.3. Acoustic model

According to some research, the equation that defines the radiated sound power is:

$$W = \rho_0 c_0 S W \sigma < \varnothing >^2; \quad (19)$$

where, $W$ is the radiated sound power in Watts, $\rho_0$ is the density of the air in kg/m$^3$, $c_0$ is the speed of sound in air in m/s, $S_W$ is the sound radiating surface in m$^2$, $\sigma$ is the radiation efficiency, and $\varnothing$ is the RMS value of the vibration velocity in m/s over the surface ($< >$) and time ($-$).

For the reactor, in the radial direction the internal and external surfaces are responsible for sound generation $S_W rad = 4\pi HR$. In the axial direction the surface responsible for radiation is the cross sectional area of the winding $S_W axi = \pi e 2R$. The radiation efficiency depends on the frequency, geometrical, and structural properties of the component. The value established for the radiation efficiency is multiplied by a correction factor to take into account all approximations made on the analytical model, neglected internal deformation, dissipation etc.

Using the considerations above, the radial and axial sound power of the winding are respectively:

$$W_{rad} = 32\rho_0 c_0 \pi^3 \mu_0^2 e_{fib}^2 \frac{f^2}{E_{fib}^2 e_{fib}^2 \varnothing^2 nbr} \cdot \left[ (R^2 + (nbr e)^2)^{1/2} - R \right]^2; \quad (20)$$

$$W_{axi} = \rho_0 c_0 \pi^2 \mu_0^2 \frac{f^2}{E_{fib}^2 e_{fib}^2} R^2 \ln(nbr) \left( e_{fib}^2 + 4\varnothing \right). \quad (21)$$

Therefore, the sound power level generated by the reactor in dB can be expressed by the following expression:

$$L_W = 10 \log_{10} \left( \frac{W_{rad} + W_{axi}}{10^{-12}} \right). \quad (22)$$

The acoustic pressure emitted by the winding in a specific point where the receiver is found depends on the comparison between the coordinates of the receiver and the dimension of the source. When the distance source-receiver $r_{sr}$ is large compared to dimensions of the source ($r_{sr}/H > 10$), the reactor is compared with a spherical source. As in most of the times the reactor is installed near the ground, the sound waves are reflected by the ground$^1$. Therefore, the reactor is comparable with a half-spherical source. The acoustic energy of internal surfaces and the power of axial modes take part in the acoustic pressure equation:

$$p = \sqrt{\frac{\rho_0 c_0 (W_{rad} + W_{axi})}{2\pi r_{sr}^2}}; \quad (23)$$

where, $r_{sr}$ is the distance from the receptor to the center of the winding.

When $r_{sr}/H < 10$, the reactor is comparable to a cylindrical source. At such distances, the participation of the noise generated by the interior wall can be neglected in front of that coming from external surface. The noise created by the axial mode may also be neglected, since its direction is parallel to the axis of the reactor.

$$p = \sqrt{\frac{\rho_0 c_0 W_{rad}}{4\pi (r_{sr} + R_e)H}}; \quad (24)$$

where $R_e$ is the external radius of the winding.

The sound pressure level $L_P$, a quantity that varies according to the environment in which the source is, can be mathematically defined as:

$$L_P = 10 \log \left( \frac{p^2}{p_0^2} \right); \quad (25)$$

where $p$ corresponds to the sound pressure in Pa and $p_0$ is $20 \times 10^{-6}$ Pa.

Sometimes, the noise created by the axial mode may not be neglected. This occurs, for example, when the reactor’s dimensions have a considerable axial area to radiate the sound.

### 3.1.4. Analytical results

Considering the geometrical properties presented at Table 1 and the equations explained in sections 3.1.1, 3.1.2, and 3.1.3 it is possible to predict the sound power level generated by this air-core reactor. For the calculations it is supposed that the

$^1$The ground is supposed to be a perfectly reflective surface, without absorption.
reactor is loaded with a single AC current of 300 Amps and a frequency of 60 Hz and the main answer will be at 120 Hz.

Young’s modulus of the aluminum and the fiberglass are \(7.2 \times 10^{10} \text{ N/m}^2\) and \(3.0 \times 10^{10} \text{ N/m}^2\), respectively. If the ratio \(r_{sr}/H < 10\), the reactor is comparable to a cylindrical source, then it is possible to use Eq. (24). The established value for the radiation efficiency is 0.25.

The sound power level calculated to this equipment was 74.3 dB and the sound pressure level estimated was 58.7 dB. In the next sections these values will be compared with numerical analysis and values determined experimentally.

3.2. Numerical Analysis

The numerical models are developed using the finite elements method. The first step of the numeric modeling was to build the geometry corresponding to the reactor analyzed in this research and mesh it. The mesh used for the structural analysis was constructed using the software Ansys 12.1. The type of the element used was shell 63. This element is defined by four nodes, four thicknesses, elastic foundation stiffness, and orthotropic material properties. Adding to that, the element has both bending and membrane capabilities. Both in-plane and normal loads are permitted. The element has six degrees of freedom at each node with translations in the nodal \(x\), \(y\), and \(z\) directions and rotations about the nodal \(x\), \(y\), and \(z\)-axes. According to the frequency of interest, the mesh was divided in 22 elements in circumferential direction and 7 elements in axial direction, see Fig. 7.

The analytical forces \(F_{\text{axial}}\) and \(F_{\text{radial}}\) calculated by analytical model were used as boundary conditions of the structural numerical model. The axial is applied above and below the mid height. The radial force is decomposed into \(x\) and \(y\) components and applied in all nodes of the model. The boundary conditions are shown in Fig. 8.

The mechanical properties defined for the structural model were: Young’s modulus of the fiberglass (10 GPa) for axial and radial directions, and Young’s modulus obtained experimentally (30 GPa) for circumferential direction. Shear modulus \(G_{xy}\) (26.7 GPa) and \(G_{xz} = G_{yz}\) (1.56 GPa) were obtained experimentally. Poisson’s ratio \(\nu_{xy}\) equals that of the aluminum (0.25). \(\nu_{xz} = \nu_{yz}\) is the same as the fiberglass (0.034). The average density was calculated, based on the area occupied by the aluminum and the fiberglass in respect to the total area of the reactor, to be 2,362 kg/m\(^3\).

For the calculations the reactor is supposed to be loaded with a single AC current of 300 Amps and frequency of 60 Hz. According to Section 2, the main answer will be at 120 Hz. The software Ansys enables the calculation of harmonic solution for the frequency of interest, Fig. 9.

The acoustic numerical model was developed to calculate the sound power level radiated by the reactor. It was developed using Boundary Element Method (BEM) available in the software Virtual.Lab 11. The mesh discretization was the same of that in the structural model. The displacements on nodes calculated in the earlier step were used for excitation in the acoustic field. In the software this boundary condition was made by the insertion of a vibrant panel. A field point mesh was created 1.0 m away from the vibration panel to obtain the...
Figure 10. (a) Vibrating panel and field point mesh and (b) the acoustic pressure at 1.0 m from vibrating panel.

pressure results. The acoustic model can be analyzed through Fig. 10a. The numerical solution enables the determination of the sound level pressure in all nodes of the mesh. The value of sound pressure 1.0 m from vibrating panel is 55 dB, Fig. 10b. The sound power level can be evaluated through this value: 69 dB.

4. EXPERIMENTAL MEASUREMENTS AND DISCUSSION

The sound power $W$ is the total sound energy emitted by a source per unit of time. To express that greatness on a scale that has a better correlation with human hearing, the sound power level $L_W$, which is related to the sound power, is given by the following equation:

$$L_W = 10 \log \left( \frac{W}{W_0} \right);$$  \hspace{1cm} (26)

where $W$ is the sound power of the source in Watts and $W_0$ is the reference power $1 \times 10^{12}$ Watts. The $L_W$ unit is dB. Using the concept of sound intensity, the equation that defines the sound power level is rewritten as follows:

$$L_W = L_P + 10 \log \left( \frac{S_m}{S_0} \right).$$ \hspace{1cm} (27)

The average value of sound pressure level in dB is $L_P$, the reference area is $S_0$, $1 \, \text{m}^2$, and $S_m$ is the surface area of measurement in $\text{m}^2$. In the case of reactors, the technical standard IEC 60076-10 specifies that the microphones must be positioned 1.0 m from its surface and the surface area of measurement should be calculated by the equation:

$$S_m = (h_{ws} + 1)l_{ms};$$ \hspace{1cm} (28)

where $h_{ws}$ corresponds to the height of the reactor without the spiders and $l_{ms}$ is the perimeter of measurement surface. The sound pressure level $L_P$, a quantity that varies according to the environment, is determined mathematically at Eq. (25).

According to standard procedure, air-core reactors with a height less than 2.5 m must be measured at the half height of the reactor for sound pressure levels. For this height, sixteen measurement positions were defined over an imaginary circumference with the center coincident with the equipment center, according to Fig. 11b. The measurements were performed in the hemi-anechoic chamber, Fig. 11a.

To do the measurements the reactor was loaded with a single AC current of 300 Amps and a frequency of 60 Hz, the main
answer was 120 Hz. At Figure 12, the average sound pressure level measured inside the hemi-anechoic chamber is presented. The sound pressure level 1.0 m from reactor was 59.7 dB and the sound power level was 73.1 dB.

Table 2 compares the results obtained analytically, numerically and experimentally. There is a strong correlation between analytical and experimental results. Comparing numerical and experimental results yields a difference around 4 dB. Considering the many assumptions, these values are reasonable.

5. CONCLUSIONS

This paper presents two relatively simple models for the evaluation of the sound power level of air-core reactors. First, the reactor is modeled as a cylinder with axial and radial displacement, and the total sound power calculated as the sum of axial and radial sound power. The developed model is general so that various air-core configurations can be applied. Second, analytical expressions are used as excitation of a structural finite element model. The results obtained through this structural model are used as boundary conditions for the acoustic boundary element model. This approach is most interesting for air-core reactors that have more than one winding.

The experimental results presented enable the identification of frequencies in which the sound power level is larger. In this region of the frequency spectrum, the vibratory energy is sufficiently high to generate relevant noise, depreciating the product.

The analytical results of the sound power level show good agreement with experimental results, thus demonstrating that the analytical model can be useful to calculate the sound pressure generated by air-core reactors. The comparison between experimental and numerical results present some differences. They are explained by the assumptions in the numerical models.

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